

Answers of sheet (1)

D. C. Generators

① SEDCG, $R_f = 100 \Omega$, $R_a = 1 \Omega$, motor constant $K = 0.5 \text{ V/Wb} \cdot \text{rad/sec}$
 $V_f = 200 \text{ V}$, $I_{\text{Load}} = 10 \text{ A}$, $N_m = 1500 \text{ rpm}$

Req:- ① E_a and V_1

② if I_{Load} doubled, $V_f = \text{const.} \rightarrow N_m = ?$ To keep V_1 the same.

①

Solution

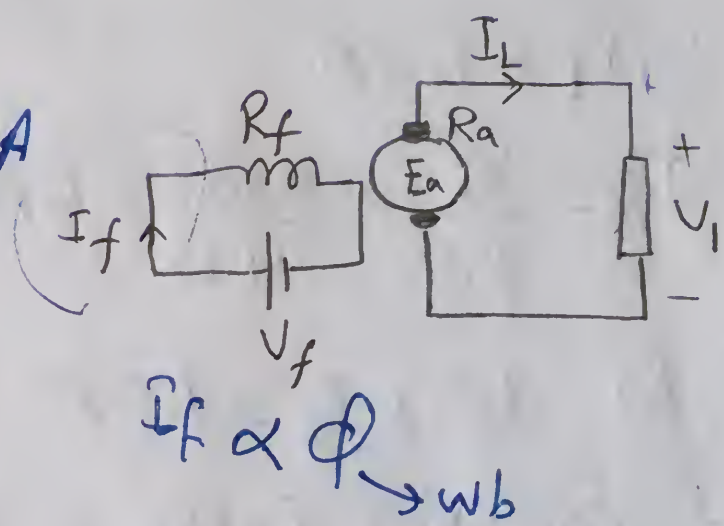
$$\therefore E_a = V_1 + I_a R_a, \quad I_a = I_L$$

$$E_a = K_v I_f \omega_m, \quad I_f = \frac{200}{100} = 2 \text{ A}$$

$$\omega_m = N_m \times \frac{\pi}{30} = 1500 \times \frac{\pi}{30} = 157.1 \frac{\text{rad}}{\text{sec.}}$$

$$\therefore E_{a1} = 0.5 \times 157.1 \times 2 = \boxed{157.1 \text{ V}}$$

$$\therefore V_1 = E_a - I_a R_a = 157.1 - 10 \times 1 = \boxed{147.1 \text{ V}}$$



②

$$I_{L2} = 2 I_{L1} = 20 \text{ A} = I_{a2}$$

$$K = \frac{0.5 \text{ V}}{\text{Wb} \cdot 1}$$

$$V_2 = V_1$$

$$\therefore E_{a2} = V_1 + I_{a2} R_a$$

$$\therefore E_{a2} = 147.1 + 20 \times 1 = \boxed{167.1 \text{ V}}$$

$$\therefore E \propto I_f \omega_m, \quad I_f \text{ const.}$$

$$\therefore \frac{E_{a1}}{E_{a2}} = \frac{I_{f1} \omega_{m1}}{I_{f2} \omega_{m2}}$$

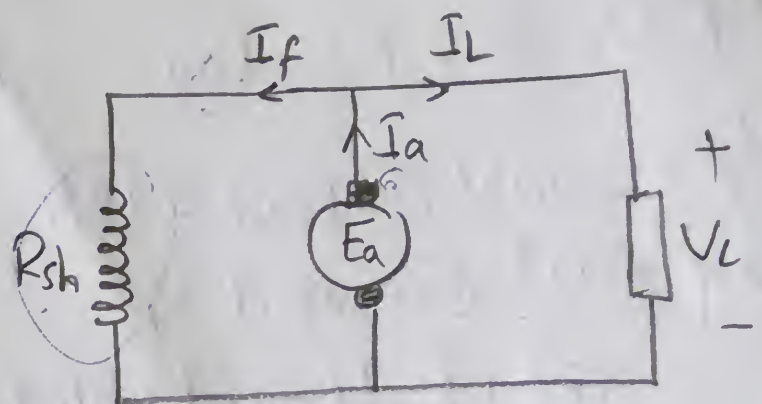
$$\therefore \omega_{m2} = \frac{E_{a2} \times \omega_{m1}}{E_{a1}} = 167.1 \frac{\text{rad}}{\text{sec}}$$

$$\therefore N_{m2} = \underline{\underline{1595.68 \text{ rpm}}}$$

② Shunt D.C.G, $P_{out} = 24 \text{ Kw} \rightarrow V_L = 200 \text{ V}$
 $R_a = 0.05 \Omega$, $R_{sh} = 40 \Omega$

Req: $P_{copper} = P_{fric} + P_{iron}$

① $P_{i/p} = ?$ ② $\eta = ?$



Solution

$$P_{out} = I_L \cdot V_L \quad \therefore I_L = \frac{P_{out}}{V_L} = \frac{24 \times 10^3}{200}$$

$$\therefore I_L = 120 \text{ A}$$

$$I_f = \frac{V_L}{R_{sh}} = \frac{200}{40} = 5 \text{ A}$$

$$\therefore I_a = I_f + I_L = 125 \text{ A}$$

$$\therefore E_a = V_L + I_a R_a = 200 + 125 \times 0.05 = 206.25 \text{ V}$$

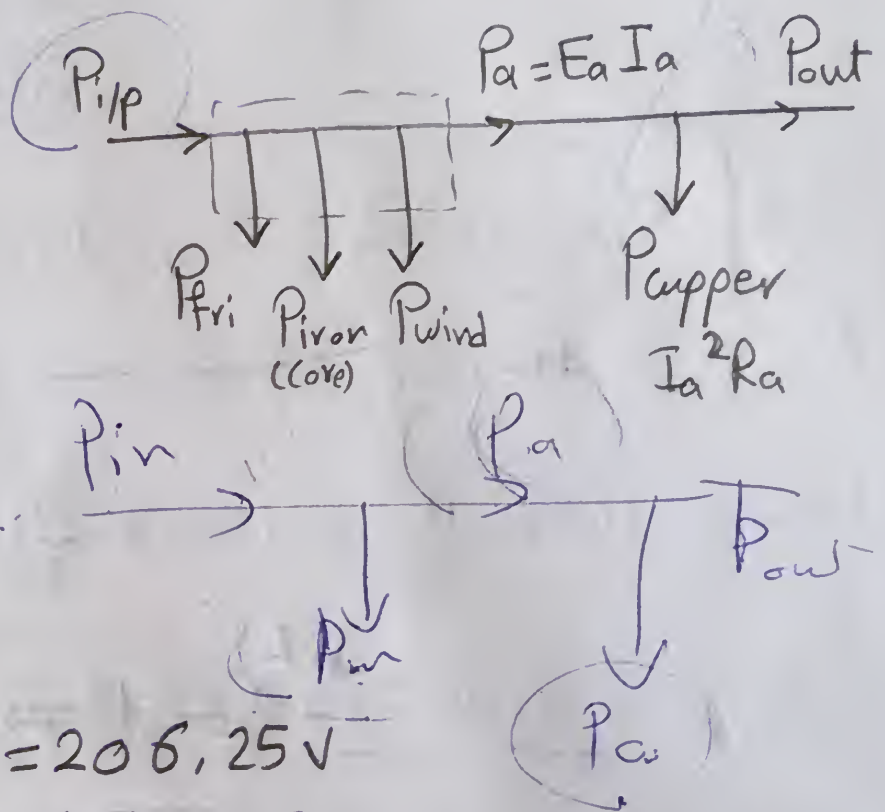
$$\therefore P_a = E_a \cdot I_a = 25.781 \text{ Kw}$$

$$\therefore P_{copper} = I_a^2 R_a + I_f^2 R_f = 1781.25 \text{ W} = P_{fric} + P_{iron}$$

$$P_{i/p} = P_a + P_{fric} + P_{iron} = P_{copper}$$

$$\therefore P_{i/p} = 27.562 \text{ Kw}$$

$$\therefore \eta = \frac{P_{o/p}}{P_{i/p}} \times 100 = 87.71 \%$$



unt D.C.G., $I_L = 100A$, $V_L = 220V$, $\eta = 0.86$
 $P_{fri} + P_{wind} + P_{core} = 1.1Kw$, $R_{sh} = 110\Omega$... Req! $R_a = ?$

Solution

$$I_f = \frac{V_L}{R_{sh}} = \frac{220}{110} = 2A$$

$$\therefore I_a = I_L + I_f = 102A$$

$$\therefore E_a = \underbrace{I_a}_{\downarrow ?} \underbrace{R_a}_{\downarrow ?} + \underbrace{V_L}_{\downarrow ?}$$

$$P_{out} = I_L \cdot V_L = 100 \times 220 = 22 Kw$$

$$\therefore \eta = 0.86 = \frac{P_{out}}{P_{in}} \therefore P_{in} = \frac{P_{out}}{\eta} = \frac{22 \times 10^3}{0.86}$$

$$\therefore P_{in} = 25.5814 Kw$$

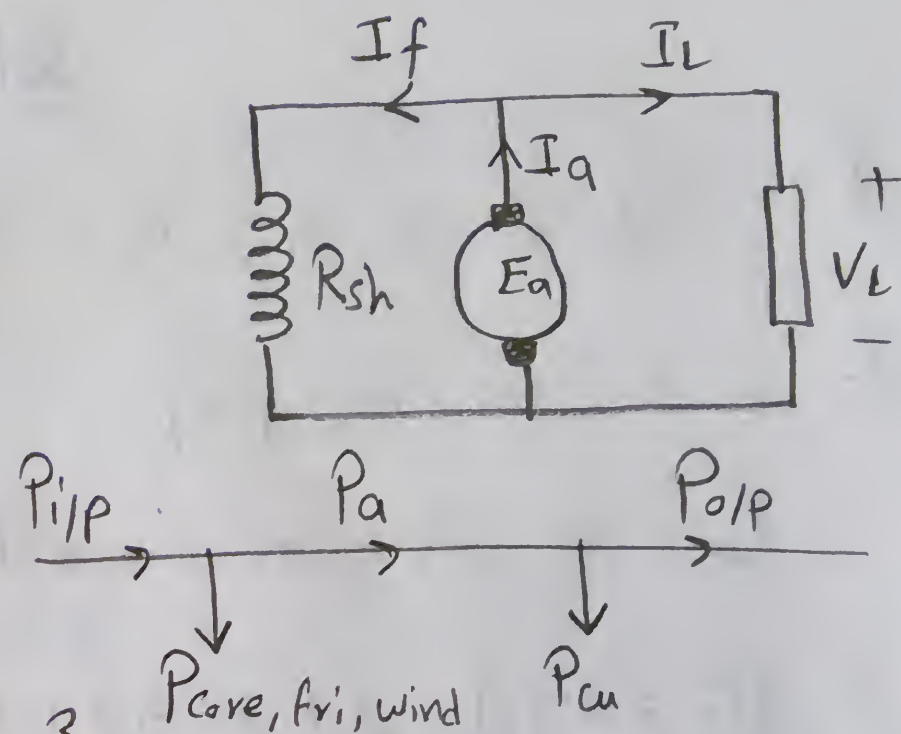
$$\therefore P_{in} = P_a + P_{core, fri, wind}$$

$$\therefore P_a = P_{in} - P_{core, fri, wind} = 24.4814 Kw$$

$$\therefore P_a = E_a I_a$$

$$\therefore E_a = \frac{P_a}{I_a} = 240V$$

$$\therefore R_a = \frac{E_a - V_L}{I_a} = \boxed{0.196\Omega \approx 0.2\Omega}$$



④ $P_{out} = 50 \text{ Kw}$, $V_L = 250 \text{ V}$, series G., $R_a = 0.02 \Omega$, $R_s = 0.045 \Omega$

$P_{stray} = 2.5 \text{ Kw}$ Req: at rated load

① I_a ② E_a ③ $P_{copper \text{ arm.}}$ ④ $P_{copper \text{ field}}$ ⑤ η

Solution

$$P_{out} = I_L \cdot V_L \quad \therefore I_L = I_a = \frac{50 \times 10^3}{250} = 200 \text{ A}$$

$$\therefore E_a = I_a (R_a + R_s) + V_L$$

$$\therefore E_a = 200 \times (0.02 + 0.045) + 250 = 263 \text{ V}$$

$$\therefore P_a = E_a I_a = 52600 \text{ watt} = 52.6 \text{ Kw}$$

$$P_{cu \text{ arm.}} = I_a^2 R_a = 800 \text{ W}$$

$$P_{cu \text{ field}} = I_a^2 R_s = 1800 \text{ W}$$

∴ from the Power flow diagram

$$\therefore P_{in} = P_{stray} + P_a = 2500 + 52600 = 55100 \text{ W} = 55.1 \text{ Kw}$$

$$\therefore P_{in} = 55.1 \text{ Kw}$$

$$\therefore \eta = \frac{50}{55.1} \times 100 = 90.7 \%$$

